
Chapter 13

Equity Valuation (Cont'd)

Expected Holding Period Return

- The return on a stock investment comprises cash dividends and capital gains or losses
 - Assuming a one-year holding period

$$\text{Expected HPR} = E(r) = \frac{E(D_1) + [E(P_1) - P_0]}{P_0}$$

Required Return

- CAPM gave us required return, call it k :
- k = market capitalization rate
- If the stock is priced correctly
 - Required return should equal expected return

$$k = r_f + \beta [E(r_M) - r_f]$$

$$k = r_f + \beta [E(r_M) - r_f]$$

=

$$\text{Expected HPR} = E(r) = \frac{E(D_1) + [E(P_1) - P_0]}{P_0}$$

Intrinsic Value

Intrinsic Value

- The present value of a firm's expected future net cash flows discounted by a risk adjusted required rate of return.

- The cash flows on a stock are?

- Dividends (D_t)

- Sale price (P_t)

$$V_0 = \frac{E(D_1) + E(P_1)}{1+k}$$

- Intrinsic Value today (time 0) is denoted V_0 and for a one year holding period may be found as:

Intrinsic Value and Market Price

- Market Price
 - Consensus value of all traders
 - In equilibrium the current market price will equal intrinsic value

- Trading Signals

- If $V_0 > P_0$

- If $V_0 < P_0$

- If $V_0 = P_0$

Buy

Sell or Short Sell

Hold as it is Fairly Priced

$$V_0 = \frac{E(D_1) + E(P_1)}{1 + k}$$

13.3 Dividend Discount Models

For now assume price = intrinsic value

Basic Dividend Discount Model

Intrinsic value of a stock can be found from the following:

$$V_0 = \sum_{t=1}^{\infty} \frac{D_t}{(1+k)^t}$$

V_0 = Intrinsic Value of Stock

D_t = Dividend in time t

k = required return

What happened to the expected sale price in this formula?

- Why is this an infinite sum?
- Is stock price independent of the investor's holding period?

Basic Dividend Discount Model

Intrinsic value of a stock can be found from the following:

$$V_0 = \sum_{t=1}^{\infty} \frac{D_t}{(1+k)^t}$$

V_0 = Intrinsic Value of Stock

D_t = Dividend in time t

k = required return

- **This equation is not useable because it is an infinite sum of variable cash flows.**
- Therefore we have to make assumptions about the dividends to make the model tractable.

No Growth Model

- Use: Stocks that have earnings and dividends that are expected to remain constant over time (zero growth)

$$V_0 = \frac{D}{k}$$

— Preferred Stock

- A preferred stock pays a \$2.00 per share dividend and the stock has a required return of 10%. What is the most you should be willing to pay for the stock?

$$V_0 = \frac{\$2.00}{0.10} = \$20.00$$

Constant Growth Model

- Use: Stocks that have earnings and dividends that are expected to grow at a constant rate forever

$$V_0 = \frac{D_0 \times (1 + g)}{k - g}; g = \text{perpetual growth rate in dividends}$$

- A common stock share just paid a \$2.00 per share dividend and the stock has a required return of 10%. Dividends are expected to grow at 6% per year forever. What is the most you should be willing to pay for the stock?

$$V_0 = \frac{\$2.00 \times 1.06}{0.10 - 0.06} = \$53.00$$

Comparing Value and Returns

- Why do you have to pay more for the constant growth stock?
 - Must pay for expected growth
- What is the one year rate of return for each stock?

No Growth Stock

$$V_0 = \$20.00$$

$$D = \$2.00$$

$$V_1 =$$

$$\$2.00 / 0.10 = \$20.00$$

$$k = \frac{\$20 - \$20 + \$2}{\$20} = 10\%$$

Constant Growth Stock

$$V_0 = \$53.00; D_0 = \$2.00$$

$$V_1 = \frac{\$2.00 \times 1.06^2}{0.10 - 0.06} = \$56.18$$

$$k = \frac{\$56.18 - \$53 + \$2.12}{\$53} = 10\%$$

Comparing Value and Returns

- Both stocks given an investor a pre-tax return of 10%.
- Is one stock a better buy than the other?

Stock Prices and Investment Opportunities

- g = growth rate in dividends is a function of two variables:
 - ROE = Return on Equity for the firm
 - b = plowback or retention percentage rate
 - (1- dividend payout percentage rate)
- $g = ROE \times b$
 g increases if a firm increases its retention ratio and/or its ROE

Value of Growth Opportunities

Value with 100% dividend payout

$$g = \text{ROE} \times b$$

Cash Cow, Inc. (CC)

$$E1 = \$5$$

$$D1 = \$5$$

$$b = 0; \text{ therefore } g = 0$$

$$k = 12.5\% ; \text{ Find } V_{\text{CC}}$$

$$V_{\text{CC}} = \frac{\$5.00}{0.125} = \$40$$

$$\text{ROE} = 12.5\%$$

Should either or both firms retain some earnings?

Growth Prospects (GP)

$$E1 = \$5 \quad V_{\text{GP}} = \frac{\$5.00}{0.125} = \$40$$

$$D1 = \$5$$

$$b = 0; \text{ therefore } g = 0$$

$$k = 12.5\%, \text{ Find } V_{\text{GP}}$$

$$\text{ROE} = 15\%$$

Value of Growth Opportunities

Value with 40% dividend payout

$$g = \text{ROE} \times b$$

Cash Cow, Inc. (CC)

$$E1 = \$5$$

7.5%

$b = 60\%$; therefore g

$$D1 = 0.40 \times \$5 = \$2.00$$

$k = 12.5\%$; Find V_{CC}

ROE = 12.5%

CC value is the same, why?

Growth Prospects (GP)

$$E1 = \$5$$

$b = 60\%$; therefore $g = 9\%$

$$D1 = 0.40 \times \$5 = \$2.00$$

$k = 12.5\%$; Find V_{GP}

ROE = 15%

GP Value has increased, why?

$$V_{CC} = \frac{2.00}{0.125 - 0.075} = \$40$$

$$V_{GP} = \frac{\$2.00}{0.125 - 0.09} = \$57.14$$

Value of Growth Opportunities

Value of assets in place for GP = \$40.00 (value with all dividends paid out, with ROE = 12.5%)

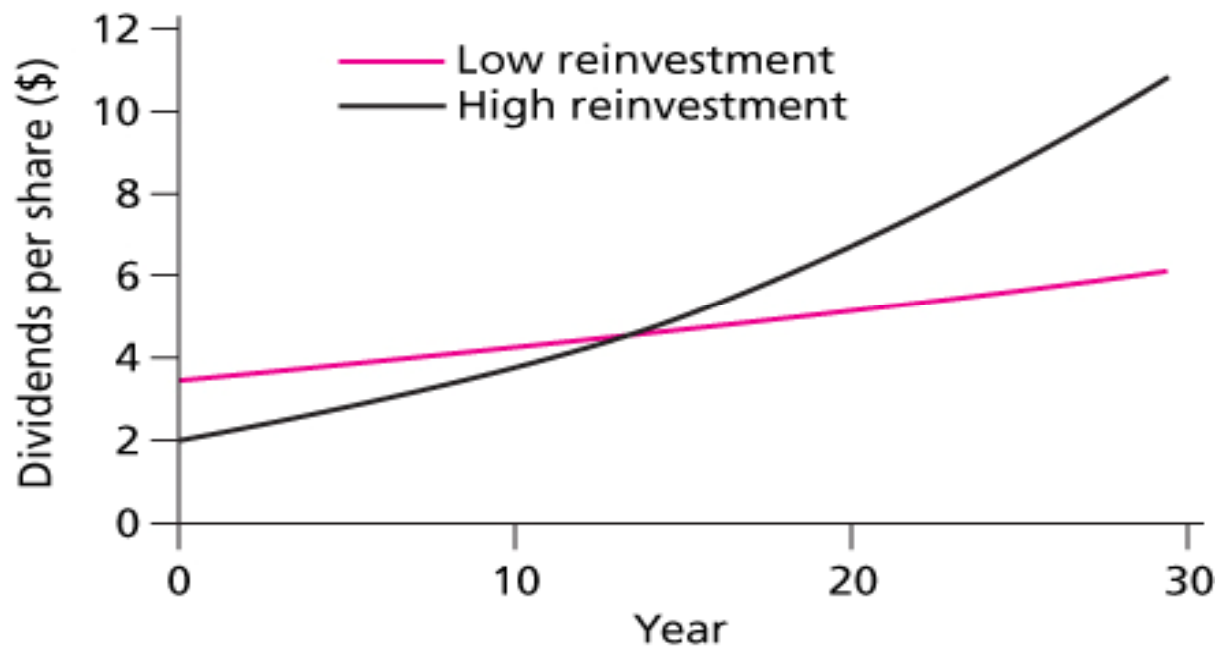
Value of growth opportunities with ROE = 15% may be inferred from the difference between the new $V_{GP} = \$57.14$ and the no growth value of \$40.00

Thus the present value of growth opportunities (PVGO) = \$57.14 - \$40.00 = \$17.14

In general:

$$PVGO = \frac{D_0(1+g)}{(k-g)} - \frac{E_1}{k}$$

Figure 13.1 Dividend Growth for Two Earnings Reinvestment Policies



(for a given ROE)
High reinvestment increases stock
price only if $ROE > k$

Multistage Growth Models

- As firms progress through their industry life cycle, earnings and dividend growth rates (ROE) are likely to change.
- A two stage growth model:

- g_1 = first growth rate
- g_2 = second growth rate
- T = number of periods of growth at g_1

$$V_0 = \left[D_0 \sum_{t=1}^T \frac{(1+g_1)^t}{(1+k)^t} \right] + \frac{D_T(1+g_2)}{(k-g_2)(1+k)^T}$$

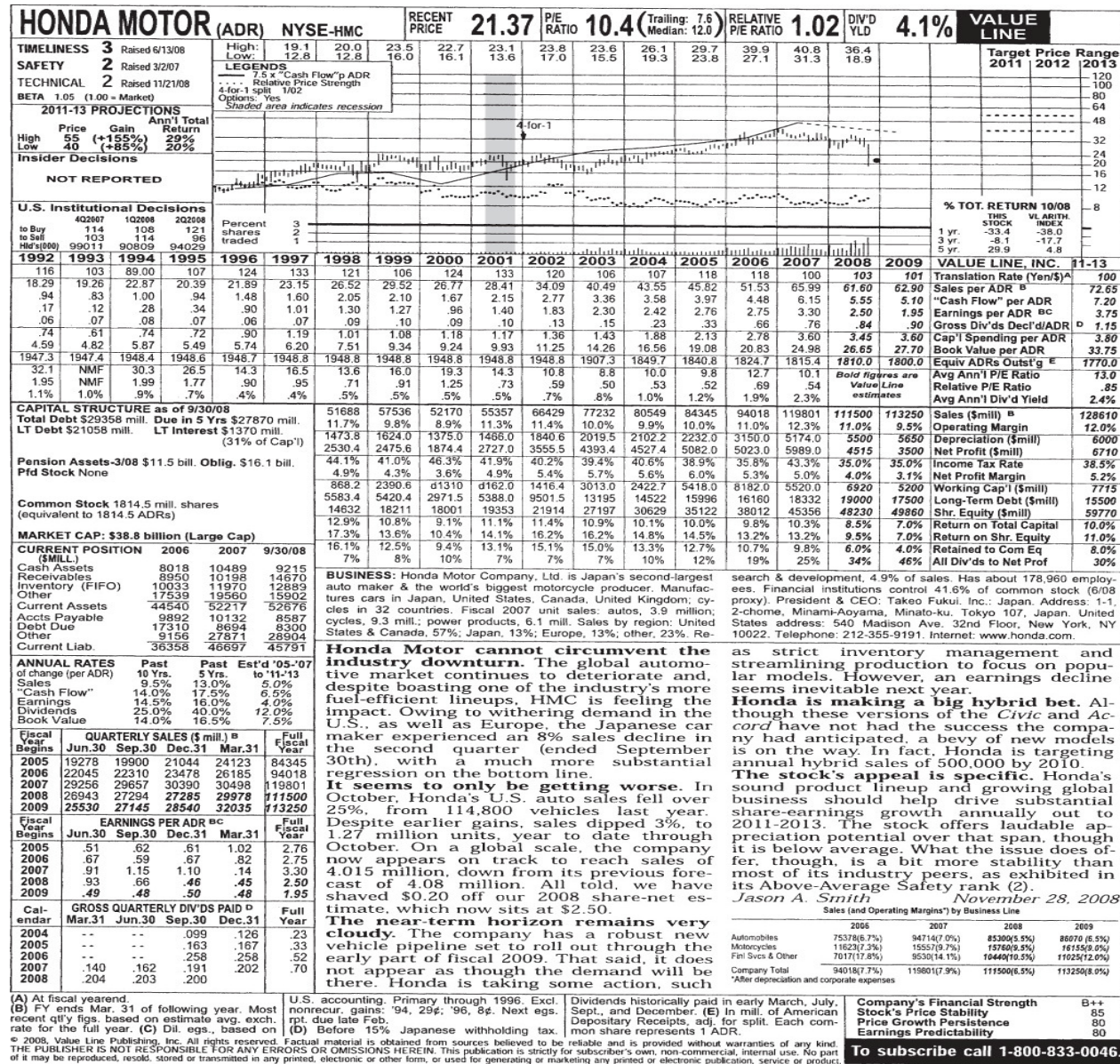
Multistage Growth Rate Model: Example

- $D_0 = \$2.00$ $g_1 = 20\%$ $g_2 = 5\%$
- $k = 15\%$ $T = 3$
- $D_1 = 2.40$ $D_2 = 2.88$ $D_3 = 3.46$ $D_4 = 3.63$

$$V_0 = \frac{\$2.40}{1.15} + \frac{\$2.88}{1.15^2} + \frac{\$3.46}{1.15^3} + \frac{\$3.63}{(0.15 - 0.05)(1.15)^3}$$

- $V_0 = 2.09 + 2.18 + 2.27 + 23.86 = \30.40

Figure 13.2 Honda Motor



Two Stage DDM for Honda

| Year | Dividend |
|------|----------|
| 2009 | 0.90 |
| 2010 | 0.98 |
| 2011 | 1.06 |
| 2012 | 1.15 |

Assume the dividend growth rate will be steady beyond 2012. Value Line forecasts $b = 70\%$ and ROE of 11.0% . What should be the long term growth rate?

$$g = \text{ROE} \times b$$

$$g = 11.0\% \times 70\% = 7.70\%$$

Two Stage DDM for Honda

The required rate of return:

$$\beta_{\text{Honda}} = 1.05 \quad \text{From Value Line}$$

$$R_f \text{ in 2008} = 3.5\%$$

Market risk premium = historical average of 8%

$$k_{\text{Honda}} = R_f + (R_M - R_f) \beta_{\text{Honda}}$$

$$k_{\text{Honda}} = 3.5\% + (8\% \times 1.05) = 11.90\%$$

Two Stage DDM for Honda

$$k = 11.90\%$$

$$g = 7.70\%$$

Find the intrinsic value

$$V_0 = \$21.88$$

$$V_0 = \frac{\$0.90}{1.119} + \frac{\$0.98}{1.119^2} + \frac{\$1.06}{1.119^3} + \frac{\$1.15}{1.119^4} + \frac{\$1.15 \times 1.077}{(0.119 - 0.077)(1.119)^4}$$

Value Line reported the actual price = \$21.37, so Honda was undervalued by \$0.51 or about 2.4%.

| Year | Dividend |
|------|----------|
| 2009 | 0.90 |
| 2010 | 0.98 |
| 2011 | 1.06 |
| 2012 | 1.15 |

Two Stage DDM for Honda

Should we trust the valuation result?

What if the beta is slightly incorrect, suppose it is 1.10 (< 5% error) rather than 1.05?

Now $k = 12.3\%$ and the intrinsic value estimate $V_0 = \$19.98$, reversing our conclusion that Honda is undervalued

Actual price = \$21.37

| Year | Dividend |
|------|----------|
| 2009 | 0.90 |
| 2010 | 0.98 |
| 2011 | 1.06 |
| 2012 | 1.15 |

13.4 Price-Earnings (P/E) Ratios

P/E Ratio and Growth Opportunities

- P/E Ratios are a function of two factors
 - Required Rates of Return (k) (inverse relationship)
 - Expected Growth in Dividends (direct relationship)
- Uses
 - Estimate intrinsic value of stocks
 - Conceptually equivalent to the constant growth DDM
 - Extensively used by analysts and investors

P/E, ROE and Growth

With positive growth: $g = \text{ROE} \times b$

$$\frac{P_0}{E_1} = \frac{(1-b)}{k-g}$$

With zero growth:

If $g = 0$ then b should $= 0$ and the ratio simplifies to:

$$\frac{P_0}{E_1} = \frac{1}{k}$$

Numerical Example: No Growth

- $E_1 = \$2.50$ $g = 0$ $k = 12.5\%$;

Find P/E and V_0

- $P/E = 1/k = 1/.125 = 8$
- $V_0 = P/E \times E_1 = 8 \times \$2.50 = \$20.00$

Numerical Example with Growth

- $b = 60\%$ $ROE = 15\%$; $k = 12.5\%$ $(1-b) = 40\%$,
 $E_0 = \$2.50$

- Find the P/E and V_0 :
- $g = ROE \times b = 15\% \times 60\% = 9\%$
- $E_1 = \$2.50 (1.09) = \2.725
- $P/E = (1 - .60) / (.125 - .09) = 11.4$
- $V_0 = P/E \times E_1 = 11.4 \times \$2.73 = \$31.14$

P/E Ratios and Stock Risk

$$\frac{P_0}{E_1} = \frac{(1-b)}{k-g}$$

- Riskier firms will have higher required rates of return (higher values of k)
- Riskier stocks will have lower P/E multiples

Pitfalls in Using P/E Ratios

- Earnings management is a serious problem,
- P/E should be calculated using pro forma earnings,
- A high P/E implies high expected growth, but not necessarily high stock returns,
- Simplistic, assumes the future P/E will not be lower than the current P/E. If expected growth in earnings fails to materialize the P/E will fall and investors may incur large losses.